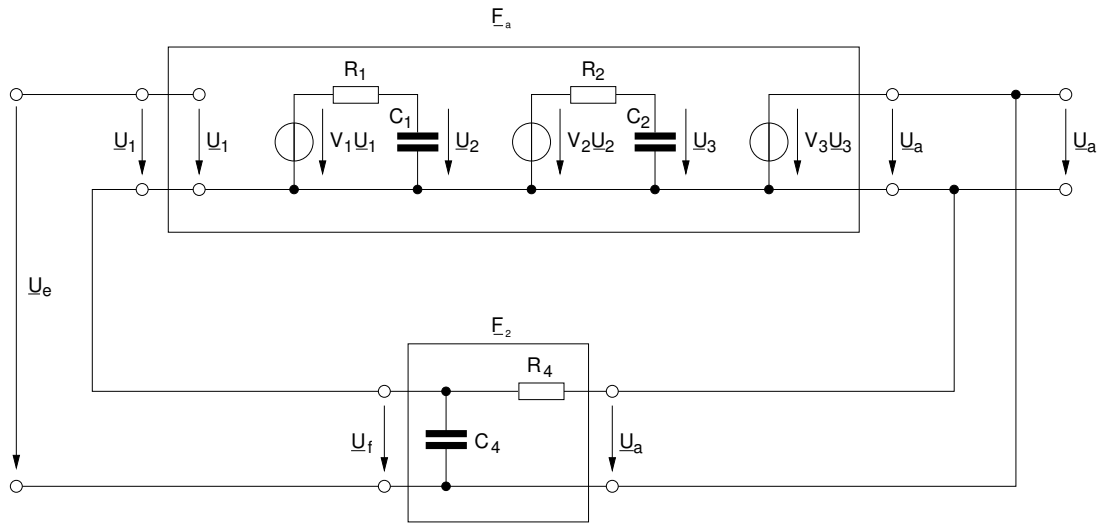




Aufgabe 1) Rückkopplung, Zweitor.

1. Frequenzgang



$$\underline{U}_e = \underline{U}_1 + \underline{U}_f \Leftrightarrow \underline{U}_1 = \underline{U}_e - \underline{U}_f$$

$$\underline{U}_a = \underline{F}_a \underline{U}_1 = \underline{F}_a \underline{U}_e - \underline{F}_a \underline{U}_f = \underline{F}_a \underline{U}_e - \underline{F}_a \underline{F}_2 \underline{U}_a \Leftrightarrow \underline{U}_a (1 + \underline{F}_a \underline{F}_2) \Leftrightarrow \underline{F} = \frac{\underline{U}_a}{\underline{U}_e} = \frac{\underline{F}_a}{1 + \underline{F}_a \underline{F}_2}$$

$$\begin{aligned} \underline{U} &= v_3 \underline{U}_3 = v_3 v_2 \frac{\frac{1}{j\omega C_2}}{R_2 + \frac{1}{j\omega C_2}} \underline{U}_2 = v_3 v_2 \frac{1}{1 + j\omega R_2 C_2} \underline{U}_2 \\ &= v_3 v_2 v_1 \frac{1}{1 + j\omega R_2 C_2} \frac{\frac{1}{j\omega C_1}}{R_1 + \frac{1}{j\omega C_1}} \underline{U}_1 \\ &= \frac{v_3 v_2 v_1}{(1 + j\omega R_1 C_1)(1 + j\omega R_2 C_2)} \underline{U}_1 \end{aligned}$$

$$\Leftrightarrow \underline{F}_a = \frac{\underline{U}_a}{\underline{U}_1} = \frac{v_0}{(1 + j\frac{\omega}{\omega_1})(1 + j\frac{\omega}{\omega_2})}$$

$$v_0 = v_1 v_2 v_3; \omega_1 = \frac{1}{R_1 C_1}; \omega_2 = \frac{1}{R_2 C_2}$$

$$\underline{U}_f = \frac{\frac{1}{j\omega C_4}}{R_4 + \frac{1}{j\omega C_4}} \underline{U}_a \Leftrightarrow \underline{F}_2 = \frac{\underline{U}_f}{\underline{U}_a} = \frac{1}{1 + j\omega R_4 C_4} = \frac{1}{1 + j\frac{\omega}{\omega_4}}; \omega_4 = \frac{1}{R_4 C_4}$$

$$\Rightarrow \underline{F}(j\omega) = \frac{\frac{v_0}{(1 + j\frac{\omega}{\omega_1})(1 + j\frac{\omega}{\omega_2})}}{1 + \frac{v_0}{(1 + j\frac{\omega}{\omega_1})(1 + j\frac{\omega}{\omega_2})(1 + j\frac{\omega}{\omega_4})}}$$

2. Stabilität von $\underline{F}_a(s)$, $\underline{F}_2(s)$

$$s = \sigma + j\omega$$

$$\underline{F}_a(s) = \frac{v_0}{\left(1 + \frac{s}{\omega_1}\right)\left(1 + \frac{s}{\omega_2}\right)} = \frac{v_0\omega_1\omega_2}{(s + \omega_1)(s + \omega_2)}$$

$$\Rightarrow s_1 = -\omega_1; s_2 = -\omega_2$$

mit $\omega_1, \omega_2 \in \mathbb{R}$ und $\omega_1, \omega_2 > 0 \Rightarrow$ Pole von $\underline{F}_a(s)$ in der LHE $\Rightarrow \underline{F}_a(s)$ ist stabil.

$$\underline{F}_2(s) = \frac{1}{1 + \frac{s}{\omega_4}} = \frac{\omega_4}{s + \omega_4}$$

$$\Rightarrow s_4 = -\omega_4$$

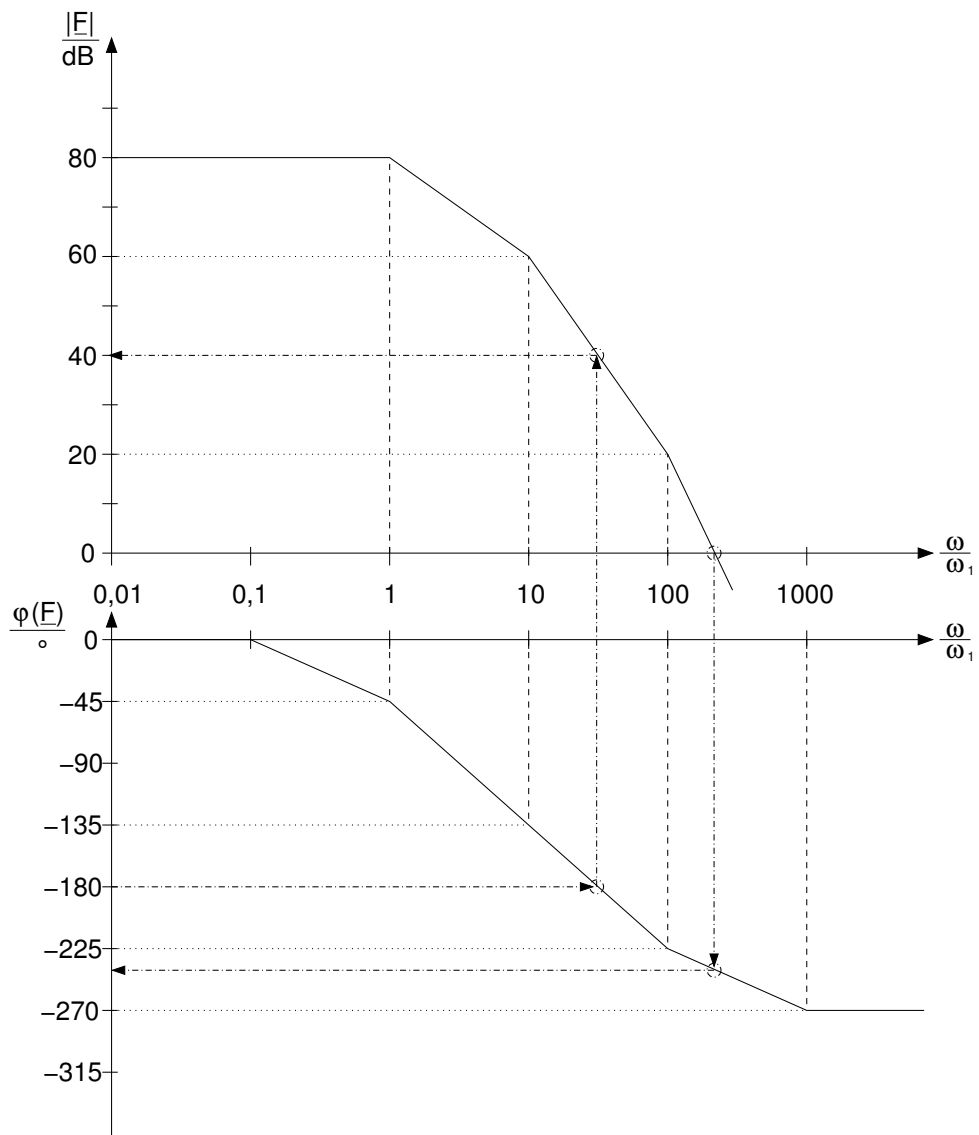
mit $\omega_4 \in \mathbb{R}$ und $\omega_4 > 0 \Rightarrow$ Pol von $\underline{F}_2(s)$ in der LHE $\Rightarrow \underline{F}_2(s)$ ist stabil.

3. Bode-Diagramm

$$\underline{F}_a \underline{F}_2 = \frac{v_0}{\left(1 + j\frac{\omega}{\omega_1}\right)\left(1 + j\frac{\omega}{\omega_2}\right)\left(1 + j\frac{\omega}{\omega_4}\right)}$$

$$|v_0| = |v_1 v_2 v_3| = 10000 = 80 \text{ dB}$$

$$100R_4C_4 = 10R_2C_2 = R_1C_1 \Leftrightarrow \frac{1}{\omega_1} = \frac{10}{\omega_2} = \frac{100}{\omega_4} \Leftrightarrow \omega_4 = 10\omega_2 = 100\omega_1$$



$$\varphi_{\text{Rand}} = 180^\circ - 238,5^\circ = -58,4^\circ < 0 \Rightarrow \text{instabil}$$

$$A_{\text{Rand}} = 40 \text{ dB} > 0 \Rightarrow \text{instabil}$$

$$\varphi_{\text{Rand}} = 0: |v_0|_{\text{dB}} = 80 \text{ dB} - 40 \text{ dB} = 40 \text{ dB}$$