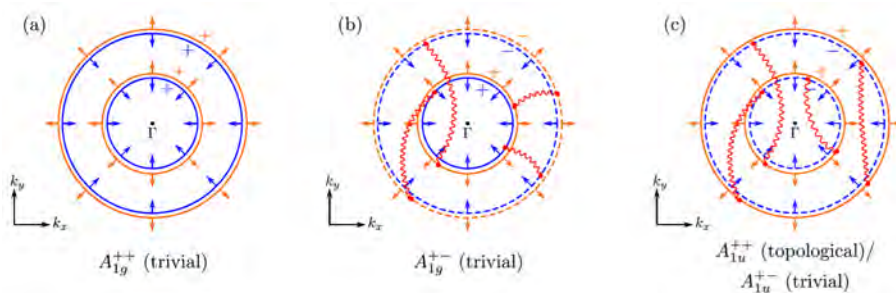


## Electron irradiation effects on superconductivity in PdTe<sub>2</sub>: An application of a generalized Anderson theorem

Peter P. Orth (Iowa State University & Ames Laboratory)

Collaboration with M. S. Scheurer, Y. Lee, L. Ke, O. Cavani, M. Konczykowski, & groups of P. Canfield and R. Prozorov

Virtual March Meeting, March 18, 2021



### References:

- E. I. Timmons *et al.*, PRR **2**, 023140 (2020)
- S. Teknowijoyo *et al.*, PRB **98**, 024508 (2018)



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# Collaborators



Theory collaborators:

- M. S. Scheurer (Harvard)
- Y. Lee, L. Ke (Ames Lab)

Experimental collaborators:

- O. Cavani, M. Konczykowski (Ecole Polytechnique)
- Groups of P. Canfield (Ames Lab) & R. Prozorov (Ames Lab)



M. S. Scheurer



L. Ke



P. Canfield



R. Prozorov

# PdTe<sub>2</sub>: crystal and electronic structure

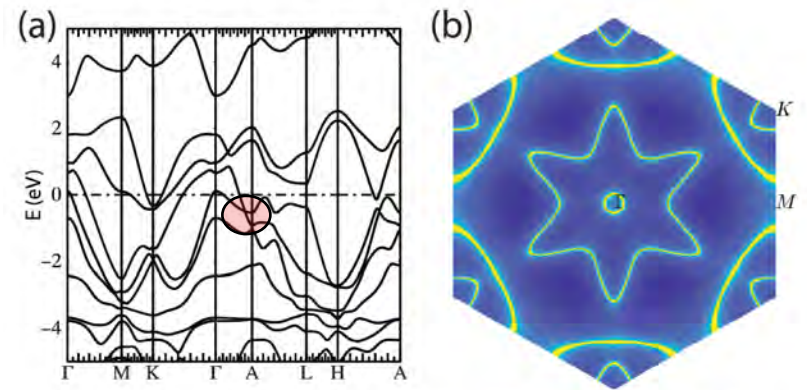
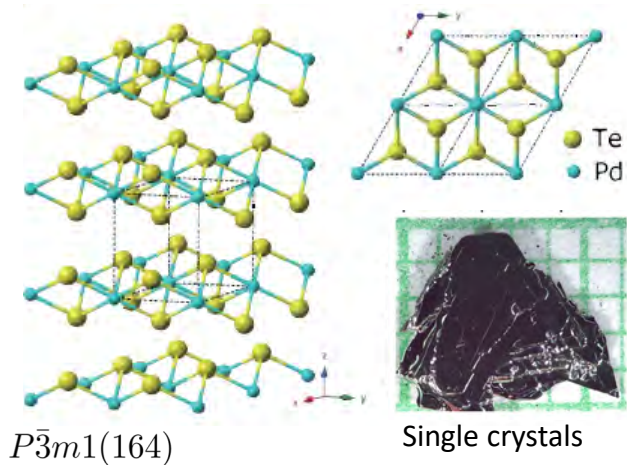


FIG. 7. (a) Band structure of PdTe<sub>2</sub>. The horizontal dot-dashed line indicates the Fermi level. (b) Fermi surface contour in PdTe<sub>2</sub> for the  $k_z = 0$  ( $\Gamma$ - $M$ - $K$ ) plane.

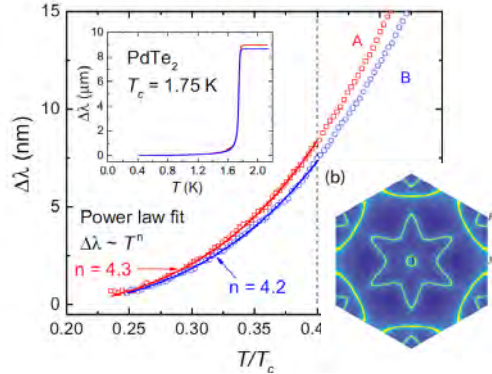
- > Centrosymmetric material,  $D_{3h}$  point group symmetry
- > Type-II Dirac semimetal: nodal point 0.5 eV below  $E_F$
- > Significant spin-orbit coupling strength
- > Fermi surface: 2 hole pockets around  $\Gamma$  and 2 electron pockets around  $K$

[1] H.-J. Noh et al., (2017).  
 [2] F. Fei et al., (2017).  
 [3] E. I. Timmons et al., (2020).  
 [4] S. Teknowijoyo et al. (2018).  
 [5] deVisser et al. (2018).

# Superconductivity in PdTe<sub>2</sub>

$$\Delta_{\mathbf{k}} = \Delta_0(\mathbf{k})i\sigma_2$$

$$\Delta_{\mathbf{k}} = \sum (\mathbf{d}_{\mathbf{k}})_j \sigma_j i\sigma_2$$


 $D_{3h}$ 

IR	Pairing	$d_n$	TRS	Order parameter $\Delta i\sigma_y$	Minimal number of nodes per FS	Topology
$A_{1g}$	$s$ wave	1	y	$a + b(X^2 + Y^2) + cZ^2$	0	trivial
$A_{2g}$	$g$ wave	1	y	$XZ(X^2 - 3Y^2)$	4 nodal lines	
$E_g$	$e_{g(1,0)}$ wave	2	y	$a(X^2 - Y^2) + bYZ$	2 nodal lines	
$E_g$	$e_{g(0,1)}$ wave	2	y	$aXY + bXZ$	2 nodal lines	
$E_g$	$e_{g(1,i)}$ wave	2	n	$a(X + iY)^2 + bZ(Y + iX)$	2 nodal points	
$A_{1u}$	$p$ wave	1	y	$a(X\sigma_x + Y\sigma_y) + bZ\sigma_z$	0	trivial/top.
$A_{2u}$	$p$ wave	1	y	$a(Y\sigma_x - X\sigma_y) + bX(X^2 - 3Y^2)\sigma_z$	2 nodal points	
$E_u$	$e_{u(1,0)}$ wave	2	y	$aX(X^2 - 3Y^2)\sigma_x + bZ\sigma_y + cY\sigma_z$	0	trivial/top.
$E_u$	$e_{u(0,1)}$ wave	2	y	$aZ\sigma_x + bX(X^2 - 3Y^2)\sigma_y + cX\sigma_z$	2 nodal points	
$E_u$	$e_{u(1,i)}$ wave	2	n	$[aZ + ibX(X^2 - 3Y^2)](\sigma_x + i\sigma_y) + c(X + iY)\sigma_z$	2 nodal points [44]	

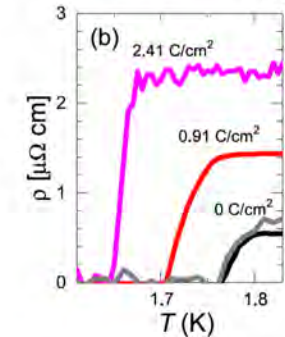
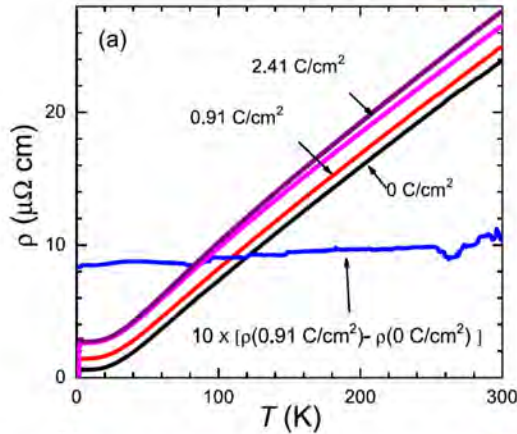
- > Superconducting (SC) transition  $T_c = 1.75$  K [1], **weak-coupling BCS & type-I SC** [2, 3]
- > **Penetration depth measurements** yield a **fully gapped** SC state [2, 3]
- > Only 3 out of 10 possible pairing states have no symmetry enforced nodes

- >  $A_{1g}$ : topologically trivial  $s$ -wave state. Could be  $A_{1g}^{++}$  or  $A_{1g}^{+-}$ .
- >  $A_{1u}$ : odd-parity  $p$ -wave state. Balian-Werthamer state on each FS.
- >  $e_{u(1,0)}$ : anisotropic odd-parity state that transforms like  $k_x$ .

Whether trivial or non-trivial depends on microscopics. Fu-Berg criterion [4] not applicable as total # of enclosed TR momenta is even.

- [1] Guggenheim et al. (1961); Hull (1965).
- [2] S. Teknowijoyo et al. (2018);
- [3] deVisser et al. (2017, 2018, 2020)
- [4] Fu, Berg (2010).

# Electron irradiation effects on superconductivity and transport



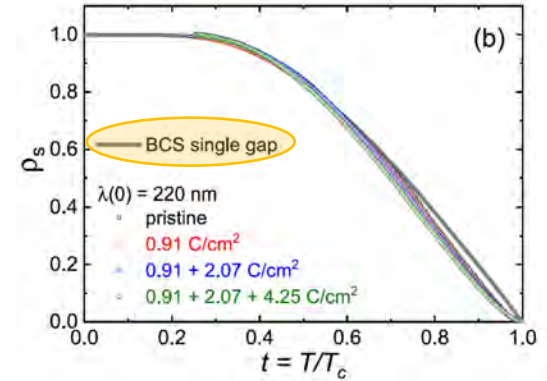
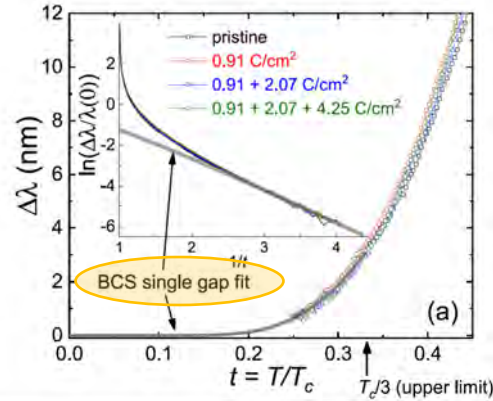
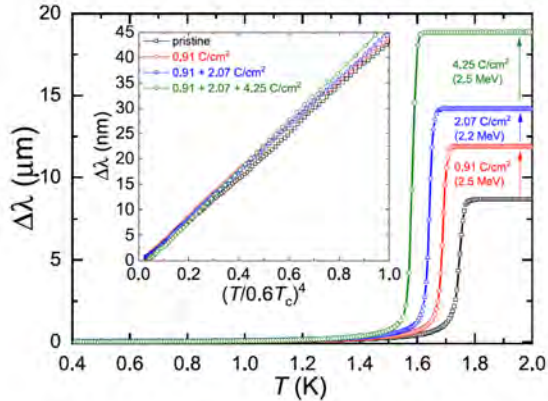
Dose ( $\text{C/cm}^2$ )	$n_e$ ( $\text{m}^{-3}$ )	$n_h$ ( $\text{m}^{-3}$ )	$\mu_e$ ( $\text{m}^2/\text{V s}$ )	$\mu_h$ ( $\text{m}^2/\text{V s}$ )	$\tau_e^{-1}$ (meV)	$\tau_h^{-1}$ (meV)	$\ell_e$ (nm)	$\ell_h$ (nm)
0	$4.2(1) \times 10^{27}$	$2.2(1) \times 10^{27}$	0.10(1)	0.28(1)	70(2)	26(2)	344(5)	725(5)
1.33	$4.2(1) \times 10^{27}$	$2.2(1) \times 10^{27}$	0.05(1)	0.14(1)	140(2)	53(2)	172(5)	363(5)

- > Electron irradiation (2.5 MeV) creates point-like defects
- > Resistivity curves shift up following Matthiessen rule
- > Carrier densities unchanged
- > Mobilities reduced by about a factor of two for 1.33  $\text{C/cm}^2$  dose
- > Superconducting  $T_c$  decreases under irradiation

[1] Timmons *et al.*, PRR (2020).



# London penetration depth under irradiation

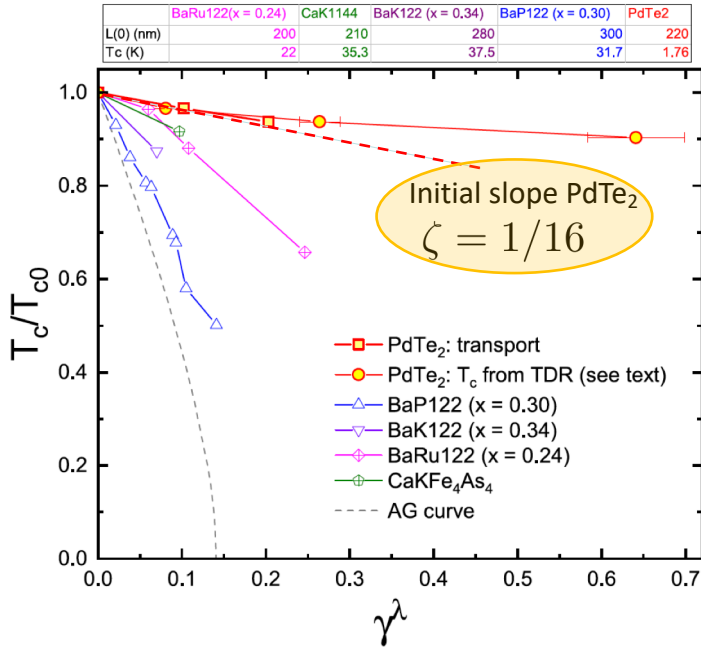


- > SC state can still be described by a **single isotropic and full gap** energy scale
  - > Sets stringent limits on degree of anisotropy required to explain  $T_c$  reduction of  $A_{1g}^{++}$  state

[1] Timmons *et al.*, PRR (2020).

# $T_c$ suppression under irradiation

Anderson (1959), Abrikosov, Gorkov (1959), Hohenberg (1964), Golubov, Mazin (1997)



Dimensionless scattering parameter:  $\gamma^\lambda = \frac{\hbar}{2\pi k_B \mu_0} \frac{\Delta \rho_0}{\lambda_0^2 T_{c,0}}$

- > Slow suppression of  $T_c$  with increased scattering
- > Initial slope  $\zeta$  of  $T_c$  suppression  $\delta T_c / T_{c,0}$ 
  - > describes fitness of SC order with respect to non-magnetic disorder
  - > Measures how many scattering events are pair breaking
  - > Yields information about pairing state
  - > Anderson theorem (isotropic s-wave):  $\delta T_c / T_{c,0} = 0$
  - > Abrikosov-Gorkov law (magnetic disorder for isotropic s-wave):  $\delta T_c / T_{c,0} = -\frac{\pi^2}{2} \gamma^\lambda$

[1] Timmons *et al.*, PRR (2020).

# Generalized Anderson theorem

Mean-field SC Hamiltonian with (non-)magnetic disorder

$$H_0 + \Delta H = \frac{1}{2} \sum_{k,k'} \Phi_{k\alpha}^\dagger (\hat{h}^{\text{BdG}})_{k\alpha,k'\alpha'} \Phi_{k'\alpha'} \leftarrow \text{Nambu spinor}$$

$$\Phi_{k\alpha} = (c_{k\alpha}, T_{\alpha\beta} c_{-k\beta}^\dagger)^T$$

BdG Hamiltonian

$$\hat{h}_n^{\text{BdG}} = \begin{pmatrix} \hat{h} & 0 \\ 0 & -\hat{h} \end{pmatrix}, \quad \text{Normal state Bloch Hamiltonian } \hat{h}_{k\alpha,k'\alpha'} = \delta_{k,k'} (\hat{h}_k)_{\alpha\alpha'}$$

$$\hat{h}_\Delta^{\text{BdG}} = \begin{pmatrix} 0 & \hat{\mathcal{D}} \\ \hat{\mathcal{D}}^\dagger & 0 \end{pmatrix}, \quad \text{SC pairing function } (\hat{\mathcal{D}})_{k\alpha,k'\alpha'} = \delta_{k,k'} (\Delta_k T^\dagger)_{\alpha\alpha'}$$

$$\hat{h}_W^{\text{BdG}} = \begin{pmatrix} \hat{W}^+ + \hat{W}^- & 0 \\ 0 & -\hat{W}^+ + \hat{W}^- \end{pmatrix}, \quad \text{Disorder:}$$

- $t_W = +$ : non-magnetic
- $t_W = -$ : magnetic



# Generalized Anderson theorem

Mean-field SC Hamiltonian with (non-)magnetic disorder

$$H_0 + \Delta H = \frac{1}{2} \sum_{\mathbf{k}, \mathbf{k}'} \Phi_{\mathbf{k}\alpha}^\dagger (\hat{h}^{\text{BdG}})_{\mathbf{k}\alpha, \mathbf{k}'\alpha'} \Phi_{\mathbf{k}'\alpha'}$$

Nambu spinor

$$\Phi_{\mathbf{k}\alpha} = (c_{\mathbf{k}\alpha}, T_{\alpha\beta} c_{-\mathbf{k}\beta}^\dagger)^T$$

BdG Hamiltonian

$$\hat{h}_n^{\text{BdG}} = \begin{pmatrix} \hat{h} & 0 \\ 0 & -\hat{h} \end{pmatrix}, \quad \text{Normal state Bloch Hamiltonian } \hat{h}_{\mathbf{k}\alpha, \mathbf{k}'\alpha'} = \delta_{\mathbf{k}, \mathbf{k}'} (\hat{h}_{\mathbf{k}})_{\alpha\alpha'}$$

$$\hat{h}_\Delta^{\text{BdG}} = \begin{pmatrix} 0 & \hat{D} \\ \hat{D}^\dagger & 0 \end{pmatrix}, \quad \text{SC pairing function } (\hat{D})_{\mathbf{k}\alpha, \mathbf{k}'\alpha'} = \delta_{\mathbf{k}, \mathbf{k}'} (\Delta_{\mathbf{k}} T^\dagger)_{\alpha\alpha'}$$

$$\hat{h}_W^{\text{BdG}} = \begin{pmatrix} \hat{W}^+ + \hat{W}^- & 0 \\ 0 & -\hat{W}^+ + \hat{W}^- \end{pmatrix}, \quad \text{Disorder:}$$

- $t_W = +$ : non-magnetic
- $t_W = -$ : magnetic

Gap unaffected by disorder if

$$[\hat{h}_n^{\text{BdG}} + \hat{h}_W^{\text{BdG}}, \hat{h}_\Delta^{\text{BdG}}]_+ = 0,$$

## Generalized Anderson theorem

$$[\hat{h}, \hat{D}]_- = 0 \quad \text{and} \quad [\hat{W}, \hat{D}]_{-t_W} = 0$$

Requires gap to be identical at points connected by disorder

$$[\Delta_s(\mathbf{k}) - t_W \Delta_{s'}(\mathbf{k}')] \langle \phi_{\mathbf{k}}^s | W | \phi_{\mathbf{k}'}^{s'} \rangle$$

Naturally holds in normal state eigenbasis

$$(\epsilon_{\mathbf{k}n} - \epsilon_{\mathbf{k}n'}) \langle \phi_{\mathbf{k}n} | \Delta_{\mathbf{k}} T^\dagger | \phi_{\mathbf{k}n'} \rangle = 0$$

Normal state eigenbasis

$$h_{\mathbf{k}} |\phi_{\mathbf{k}n}\rangle = \sigma_0 \epsilon_{\mathbf{k}n} |\phi_{\mathbf{k}n}\rangle$$

# Pair breaking scattering & disorder sensitivity

Pair breaking scattering between points where gap is not identical

$$C_{ks,k's'} := [\Delta_s(\mathbf{k}) - t_W \Delta_{s'}(\mathbf{k}')] \langle \phi_{\mathbf{k}}^s | W | \phi_{\mathbf{k}'}^{s'} \rangle$$

- $t_W = +$ : non-magnetic disorder
- $t_W = -$ : magnetic disorder

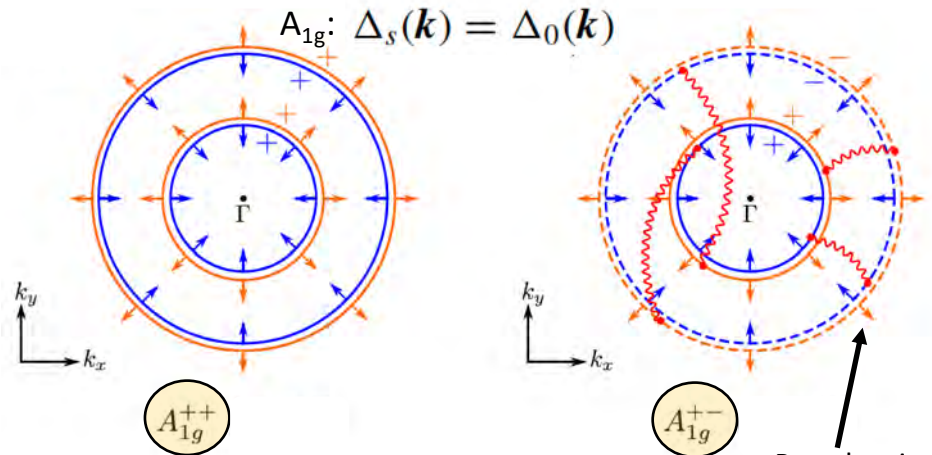
> SC disorder sensitivity parameter

$$\zeta = \frac{\sum_{\mathbf{k}, \mathbf{k}'}^{\text{FS}} \sum_{s, s'} |C_{ks, k's'}|^2}{2 \text{tr}[W^\dagger W] \sum_{\mathbf{k}}^{\text{FS}} \sum_s |\Delta_s(\mathbf{k})|^2}$$

FS average of violation of generalized Anderson theorem

> Slope of  $T_c$  suppression determined by  $\zeta$

$$\delta T_c / T_{c,0} \sim -\frac{\pi}{4T_{c,0}} \tau^{-1} \zeta$$



SC order parameter

$$\langle \phi_{\mathbf{k}'}^{s'} | \Delta_{\mathbf{k}} (i\sigma_2)^\dagger | \phi_{\mathbf{k}}^s \rangle = \delta_{s,s'} \Delta_s(\mathbf{k})$$

$$A_{1g}: \Delta_s(\mathbf{k}) = \Delta_0(\mathbf{k})$$

Normal state eigenbasis

$$h_{\mathbf{k}} | \phi_{\mathbf{k}n} \rangle = \sigma_0 \epsilon_{\mathbf{k}n} | \phi_{\mathbf{k}n} \rangle$$

# Disorder sensitivity parameter

- > SC disorder sensitivity parameter

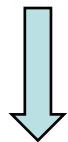
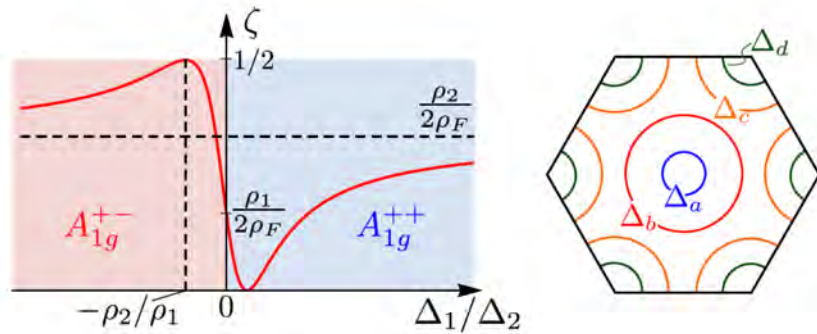
$$\zeta = \frac{\sum_{\mathbf{k}, \mathbf{k}'}^{\text{FS}} \sum_{s, s'} |C_{\mathbf{k}s, \mathbf{k}'s'}|^2}{2 \text{tr}[W^\dagger W] \sum_{\mathbf{k}}^{\text{FS}} \sum_s |\Delta_s(\mathbf{k})|^2}.$$

- > Slope of  $T_c$  suppression determined by  $\zeta$

$$\delta T_c / T_{c,0} \sim -\frac{\pi}{4T_{c,0}} \tau^{-1} \zeta$$

Abrikosov, Gorkov (1959), Hohenberg (1964), Golubov, Mazin (1997), Cavanagh, Brydon (2020), Michaeli, Fu (2012), Scheurer (2016); Timmons *et al.* (2020).

## Isotropic multi-band SC



Density of states of pocket  $n$

$$\zeta = \frac{1}{2} \left[ 1 - \frac{(\sum_n \rho_n \Delta_n)^2}{(\sum_n \rho_n \Delta_n^2) \sum_n \rho_n} \right].$$

Timmons *et al.*, PRR (2020).

# Gap anisotropies in PdTe<sub>2</sub> required for observed T<sub>c</sub> suppression

$$v = \frac{\sum_{n \in C_1} \rho_n}{(\sum_n \rho_n - \sum_{n \in C_1} \rho_n)}$$

C <sub>1</sub>	v	(Δ <sub>1</sub> /Δ <sub>2</sub> ) <sub>1</sub>	(Δ <sub>1</sub> /Δ <sub>2</sub> ) <sub>2</sub>
{a}	7.5 × 10 <sup>-3</sup>	5.6	-3.3
{b}	0.40	2.1	0.32
{c}	2.1	2.8	0.48
{d}	0.034	3.3	-0.98
{a, b}	0.41	2.1	0.33
{a, c}	2.1	2.8	0.48
{a, d}	0.042	3.1	-0.78
{c, d}	2.4	3.0	0.47

> A<sub>1g</sub><sup>++</sup> requires Δ<sub>1</sub>/Δ<sub>2</sub> = 2.1

Substantial anisotropy necessary for A<sub>1g</sub><sup>++</sup> state to be consistent with T<sub>c</sub> suppression

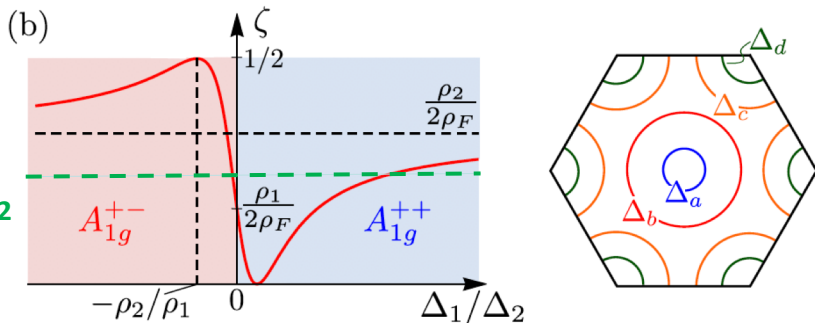
> A<sub>1g</sub><sup>+−</sup> can be isotropic Δ<sub>1</sub>/Δ<sub>2</sub> = −0.98

Unconventional isotropic A<sub>1g</sub><sup>+−</sup> state is most likely candidate.

$$\Delta_a = \Delta_b = \Delta_c = \Delta_2, \Delta_d = \Delta_1.$$

Sign change between three inner and small outer most pocket at K point.

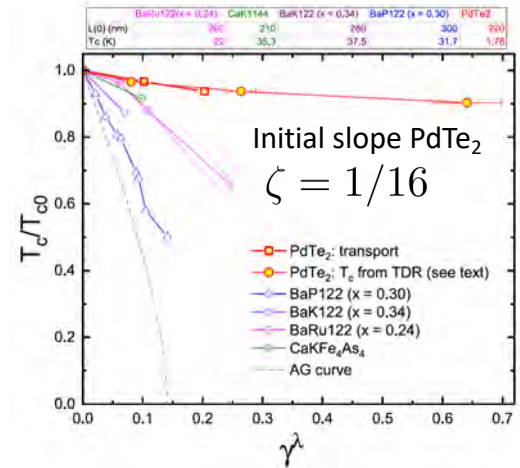
Timmons et al., PRR (2020).



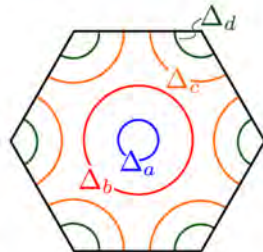
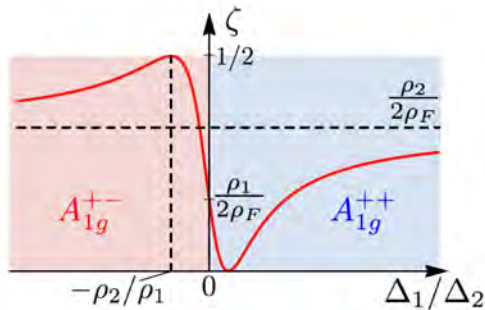
Experimental value for PdTe<sub>2</sub>  
ζ = 1/16

# Summary

- > Penetration depth  $\lambda \gg$  single isotropic full SC gap
- > Slow but finite  $T_c$  suppression under electron irradiation  $\gg \zeta = \frac{1}{16}$
- > Minimal required anisotropy for  $s^{++}$  state:  $\Delta_1/\Delta_2 \approx 2.1$
- > Minimal required anisotropy for  $s^+$  state:  $\Delta_1/\Delta_2 \approx -0.98$



➡ Unconventional  $A_{1g}^{+-}$  state more likely than  $A_{1g}^{++}$  due to weak observed anisotropy.



## References:

- E. I. Timmons *et al.*, PRR **2**, 023140 (2020)
- S. Teknowijoyo *et al.*, PRB **98**, 024508 (2018)

Thank you for your attention!

# Disorder sensitivity parameter

- > SC disorder sensitivity parameter

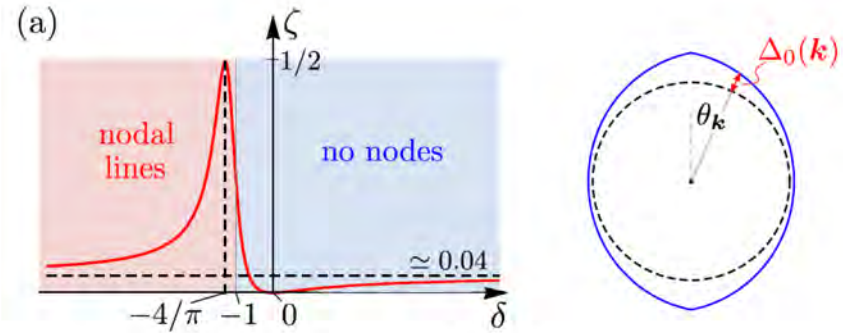
$$\zeta = \frac{\sum_{\mathbf{k}, \mathbf{k}'}^{\text{FS}} \sum_{s, s'} |C_{\mathbf{k}s, \mathbf{k}'s'}|^2}{2 \text{tr}[W^\dagger W] \sum_{\mathbf{k}}^{\text{FS}} \sum_s |\Delta_s(\mathbf{k})|^2}.$$

- > Slope of  $T_c$  suppression determined by  $\zeta$

$$\delta T_c / T_{c,0} \sim -\frac{\pi}{4T_{c,0}} \tau^{-1} \zeta$$

Abrikosov, Gorkov (1959), Hohenberg (1964), Golubov, Mazin (1997), Cavanagh, Brydon (2020), Michaeli, Fu (2012), Scheurer (2016); Timmons *et al.* (2020).

## Anisotropic s-wave



$$\Delta_0(\mathbf{k}) = \Delta_0[1 + \delta \sin(\theta_{\mathbf{k}})]$$

$$\Rightarrow \zeta = \frac{(32 - 3\pi^2)\delta^2}{16(6 + 3\pi\delta + 4\delta^2)}.$$

Timmons *et al.*, PRR (2020).