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**Title:** Multivariable versions Kaluza's Lemma.

**Abstract:** Let  $d \in \mathbb{N}$  and  $f(z) = \sum_{\alpha \in \mathbb{N}_0^d} c_\alpha z^\alpha$  be a convergent multivariable power series in  $z = (z_1, \dots, z_d)$ . We present two independent conditions on the positive coefficients  $c_\alpha$  which imply that  $f(z) = \frac{1}{1 - \sum_{\alpha \in \mathbb{N}_0^d} q_\alpha z^\alpha}$  for non-negative coefficients  $q_\alpha$ . It turns out that functions of the type

$$f(z) = \int_{[0,1]^d} \frac{1}{1 - \sum_{j=1}^d t_j z_j} d\mu(t)$$

satisfy one of our conditions, whenever  $d\mu(t) = d\mu_1(t_1) \times \dots \times d\mu_d(t_d)$  is a product of probability measures  $\mu_j$  on  $[0, 1]$ . The results have applications in the theory of Nevanlinna-Pick kernels.

The motivations for both conditions are similar. Yet, the calculation for the second condition is using non-commutative function theory. This is joint work with Jesse Sautel.